

3. To define  $b_3(m)$ , for each  $v' \in V$  in the case of  $u \neq 0$  first define:

$$b_{3,v'}(m) := \begin{cases} 1, & \text{if } (v, v') \in E \\ & \text{and } \exists B' \in \mathcal{B}_{v'}: |B_u \cap B'| \neq 0 \\ & \text{and } \forall B' \in \mathcal{B}_{v'}: B_u \neq B'; \\ 0, & \text{in all other cases.} \end{cases}$$

In the case of  $u \neq 0$  further define:

$$g := \left| \{v' \in V \mid (v, v') \in E, \exists B' \in \mathcal{B}_{v'}: |B_u \cap B'| \neq 0\} \right|.$$

Now set:

$$b_3(m) := \begin{cases} \frac{\sum_{v' \in V} b_{3,v'}(m)}{g}, & \text{if } u \neq 0 \text{ and } g > 0; \\ 0, & \text{otherwise.} \end{cases}$$

Interpretation: The sum  $\sum_{v' \in V} b_{3,v'}(m)$  measures the number of possible SFN-situations, the source ensemble  $B_u$  of the elementary move  $m$  could make use of, but has not yet done so. In our context, we understand a SFN-situation to be any two adjacent and equal ensembles. We obtain the value  $b_3(m)$  from  $\sum_{v' \in V} b_{3,v'}(m)$  by dividing out the problem size appropriate and represented by the value  $g$ .

Having introduced  $b_1(m)$ ,  $b_2(m)$  and  $b_3(m)$ , we can now define the relations “ $\equiv$ ” and “ $\triangleleft$ ”. For this, let again  $\mathcal{B}$  be an ensemble assignment, and let  $m_1, m_2 \in M(\mathcal{B})$  be two elementary moves on  $\mathcal{B}$ .

1. We say that  $m_1$  and  $m_2$  are equivalent,  $m_1 \equiv m_2$ , if  $\exists i \in \{1, \dots, 3\}$  that the following property holds:

$$(b_j(m_1) = b_j(m_2) = 0 \text{ for } j = 1, \dots, i-1) \text{ and } \begin{cases} b_i(m_1) = b_i(m_2) > 0, & \text{if } i < 3. \\ b_i(m_1) = b_i(m_2) \geq 0, & \text{if } i = 3. \end{cases}$$

2. We say that  $m_1$  is smaller than  $m_2$ ,  $m_1 \triangleleft m_2$ , if  $\exists i \in \{1, \dots, 3\}$  that the following property holds:

$$(b_j(m_1) = b_j(m_2) = 0 \text{ for } j = 1, \dots, i-1) \text{ and } b_i(m_1) < b_i(m_2).$$